

Operational Amplifier [Op-Amp]

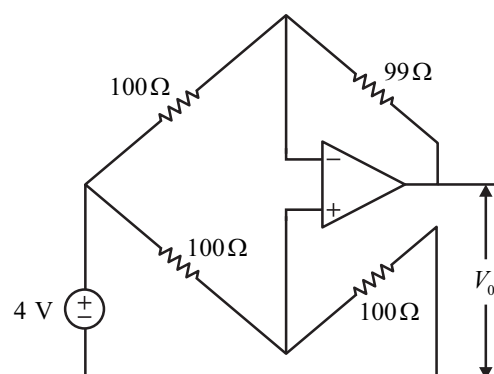
Answer Keys, Solutions and Corrections

1. BASIC IDEAL & PRACTICAL OP-AMP :

1.1	D	1.2	- 4	1.3	C, D	1.4	D	1.5	B
1.6	0.02	1.7	D	1.8	C	1.9	C	1.10	D
1.11	A	1.12	D	1.13	D	1.14	A	1.15	B
1.16	D	1.17	D	1.18	C, D	1.19	D	1.20	D
1.21	D	1.22	A	1.23	B	1.24	C	1.25	A
1.26	B	1.27	B	1.28	B	1.29	D	1.30	B
1.31	D	1.32	A	1.33	C	1.34	D	1.35	B
1.36	C	1.37	C	1.38	B	1.39	A	1.40	B
1.41	A	1.42	A	1.43	B	1.44	B	1.45	B
1.46	C	1.47	A	1.48	B	1.49	B	1.50	C
1.51	B	1.52	A	1.53	B	1.54	C	1.55	B
1.56	A	1.57	D	1.58	B	1.59	A	1.60	A
1.61	B	1.62	A	1.63	C	1.64	C	1.65	B
1.66	C	1.67	D	1.68	B	1.69	0.6	1.70	12
1.71	250	1.72	1	1.73	1.39	1.74	B	1.75	B
1.76	-1	1.77	100	1.78	100	1.79	D	1.80	D
1.81	C	1.82	B	1.83	C	1.84	B	1.85	B

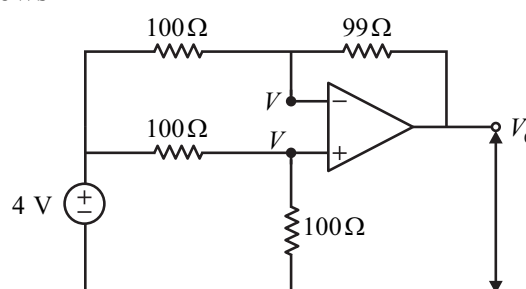
1.6 For the ideal Op-Amp circuit of figure. Determine the output voltage V_0

[GATE EC 1993, IIT-Bombay]



Ans. 0.02 V

Sol. Circuit will reduce as follows



Due to virtual ground condition

$$V_+ = V_- = V$$

Apply KCL at non-inverting terminals

$$\frac{V-4}{100} + \frac{V}{100} = 0$$

$$\frac{2V}{100} = \frac{4}{100} \Rightarrow V = 2 \text{ Volts}$$

Apply KCL at inverting terminal

$$\frac{V-4}{100} + \frac{V-V_0}{99} = 0$$

Put $V = 2$ Volts.

$$\frac{2-4}{100} + \frac{2-V_0}{99} = 0$$

$$\frac{2-V_0}{99} = \frac{2}{100}$$

$$200 - 100V_0 = 198$$

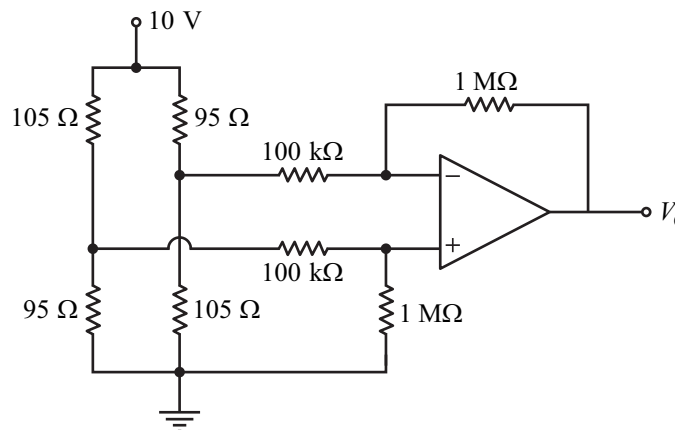
$$100V_0 = 2$$

$$V_0 = 0.02 \text{ Volt}$$

1.8 Correction Option (C) $1 + \frac{R_f}{R}$

1.55 For the Op-Amp circuit shown below, V_0 is approximately equal to

[GATE IN 2008, IIT-Bangalore]



(A) -10 V

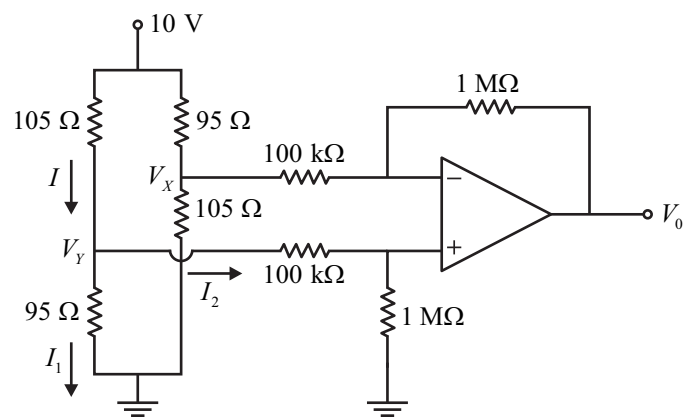
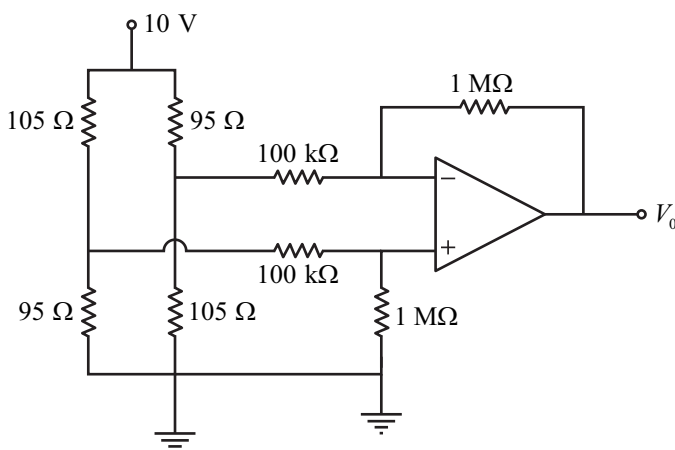
(B) -5 V

(C) +5 V

(D) +10 V

Ans. (B)

Sol.



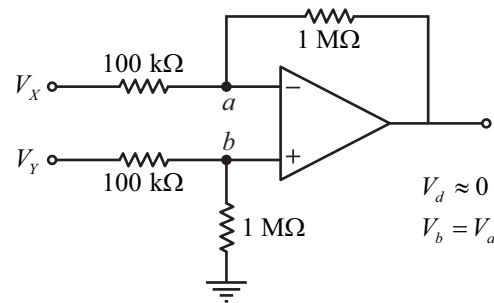
$$V_x = 10 \left(\frac{105}{200} \right) = 5.25 \text{ V}$$

$$I = I_1 + I_2$$

$$I_1 \gg I_2 \quad [\text{Due to small resistance } 95 \Omega]$$

⇒ 95 Ω and 105 Ω will be in series

$$V_y = 10 \left(\frac{95}{200} \right) = 4.75 \text{ V} \quad [\text{By VDR}]$$



Apply KCL at 'b'

$$\frac{V_y - V_b}{100} = \frac{V_b}{1000} \quad \Rightarrow \quad 10V_y = 11V_b$$

$$V_b = \left(\frac{10}{11} \right) V_y = 4.31817 \text{ Volts}$$

Apply KCL at 'a'

$$\frac{V_x - V_a}{100} = \frac{V_a - V_o}{1000}$$

$$10V_x = 11V_a - V_o$$

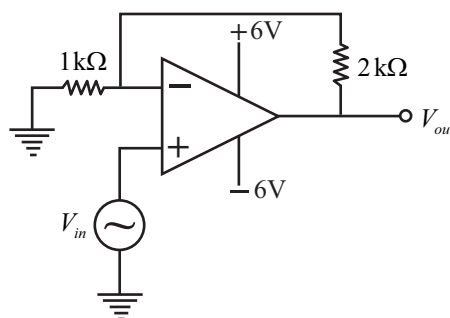
$$V_o = 11V_a - 10V_x$$

$$V_o = 10(4.31817) - 10(5.25) = 47.5 - 52.5$$

$$V_o = -5 \text{ V}$$

1.58 The nature of feedback in the Op-Amp circuit shown is

[GATE EE 2009, IIT-Roorkee]



(A) Current - Current feedback

(B) Voltage - Voltage feedback

(C) Current - Voltage feedback

(D) Voltage - Current feedback

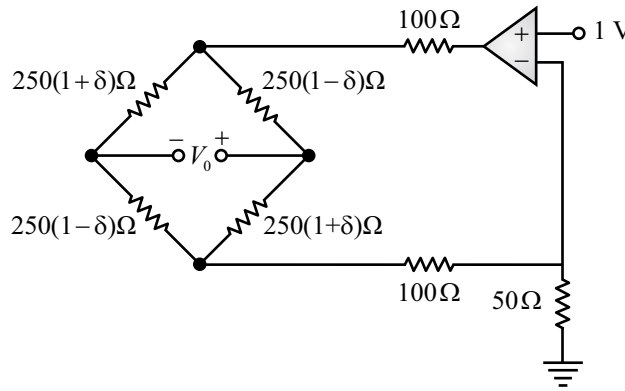
Ans. (B)

Sol. (i) Voltage (sampling) + Series (mixing) feedback

(ii) Series (mixing) + Shunt (sampling) feedback

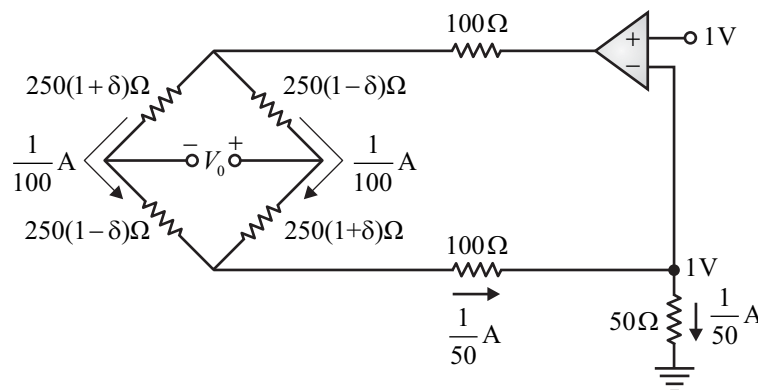
(iii) Voltage (sampling) + Voltage (mixing) feedback

1.71 In the circuit shown, assume that the Op-Amp is ideal. The bridge output voltage V_0 (in mV) for $\delta = 0.05$ is _____ .
 [GATE EC 2015 (Set-01), IIT-Kanpur]



Ans. (250)

Sol.



Due to virtual ground concept

$$V_+ = V_- = 1V$$

Current in $100\ \Omega$ and $50\ \Omega$ resistor will be same

$$I_{50\Omega} = I_{100\Omega} = \frac{1}{50}\text{ A}$$

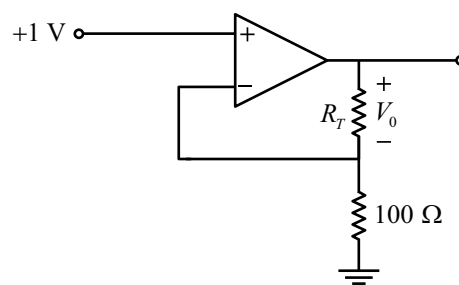
So, output voltage is given by,

$$V_0 = \frac{1}{100} [250(1+\delta) - 250(1-\delta)] = \frac{1}{100} \times 500\delta$$

$$V_0 = 5\delta = \delta \times 0.05 = 0.25\text{ V}$$

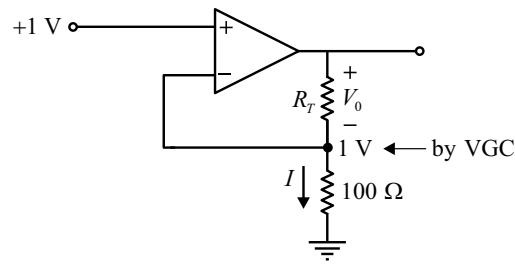
$$V_0 = 250\text{ mV}$$

1.73 In the figure shown, R_T represents a resistance temperature device (RTD), whose characteristic is given by $R_T = R_0(1 + \alpha T)$, where $R_0 = 100\ \Omega$, $\alpha = 0.0039^\circ\text{C}^{-1}$ and T denotes the temperature in $^\circ\text{C}$. Assuming the op-amp to be ideal, the value of V_0 in volts when $T = 100^\circ\text{C}$, is _____ V.
 [GATE IN 2015, IIT-Kanpur]



Ans. (1.39 V)

Sol.



Given : $\alpha = 0.0039^\circ\text{C}^{-1}$, $R_0 = 100$, $T = 100^\circ\text{C}$

$$R_T = R_0(1 + \alpha T) = 100(1 + 0.0039 \times 100)$$

$$R_T = 139 \Omega$$

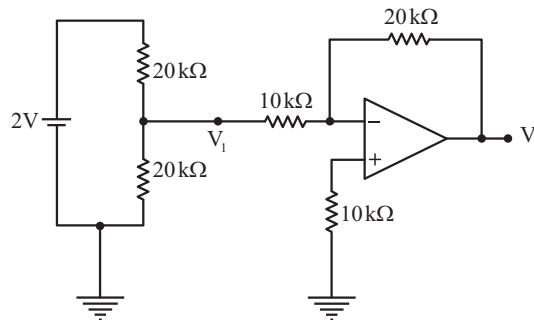
$$I = \frac{1}{100} \text{ A}$$

$$V_0 = I \times R_T = 139 \times \frac{1}{100}$$

$$V_0 = 1.39 \text{ V}$$

1.76 In the circuit given below, the OP-AMP is ideal. The output voltage V_0 in volt is _____.

[GATE IN 2016, IISc Bangalore]



Sol.

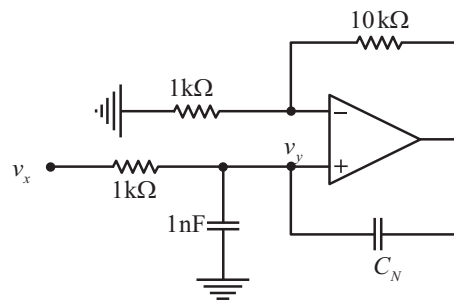
$$\frac{V_1 - 2}{20} + \frac{V_1}{20} + \frac{V_1}{10} = 0$$

$$V_1 = 0.5 \text{ V}$$

$$V_0 = \frac{-20}{10} \times 0.5 = -1 \text{ V}$$

1.77 In the circuit given below, the OP-AMP is ideal. The input v_x is a sinusoid. To ensure $v_y = v_x$, the value of C_N in picofarad is _____

[GATE IN 2016, IISc Bangalore]



Sol. Applying KCL at inverting terminal,

$$\frac{V_y - 0}{1 \text{ k}\Omega} + \frac{V_y - V_0}{10 \text{ k}\Omega} = 0$$

$$\frac{V_y}{1} + \frac{V_y}{10} = \frac{V_0}{10}$$

$$V_0 = 11 V_y$$

... (i)

Applying KCL at non-inverting terminal,

$$\frac{V_y - V_x}{1 \text{ k}\Omega} + \frac{V_y}{sC} + \frac{V_y - V_0}{sC_N} = 0$$

$$V_y \cdot sC + (V_y - 11 V_y) \cdot sC_N = 0$$

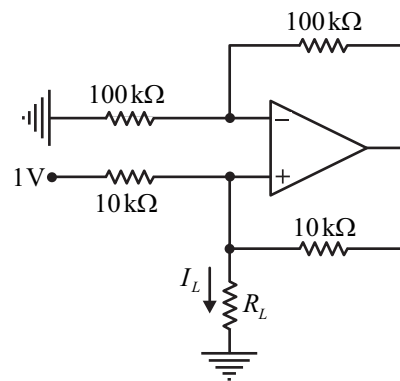
$$V_y \cdot sC - 10 V_y \cdot sC_N = 0$$

$$V_y \cdot sC = 10 V_y \cdot sC_N$$

$$C_N = \frac{C}{10} = 0.1 \text{ nF} = 100 \text{ pF}$$

1.78 In the circuit given below, the OP-AMP is ideal. The value of current I_L in microampere is _____

[GATE IN 2016, IISc Bangalore]



Sol. Applying KCL at inverting terminal,

$$\frac{V - 0}{100 \text{ K}} + \frac{V - V_0}{100 \text{ K}} = 0$$

$$\frac{2V}{100 \text{ K}} = \frac{V_0}{100 \text{ K}}$$

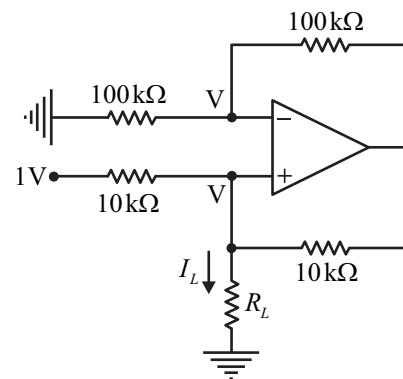
$$V_0 = 2V$$

Applying KCL at non inverting,

$$\frac{V - 1}{10 \text{ K}} + I_L + \frac{V - V_0}{10 \text{ K}} = 0$$

$$\frac{V}{10 \text{ K}} - \frac{1}{10 \text{ K}} + I_L - \frac{V}{10 \text{ K}} = 0$$

$$I_L = 0.1 \text{ mA} = 100 \mu\text{A}$$



1.81 In an Op-Amp, if the feedback voltage is reduced by connecting a voltage divider at the output, which of the following will happen? [IES EC 2016]

1. Input impedance increases
2. Output impedance reduces
3. Overall gain increases

Which of the above statements is/are correct?

- (A) 1 only (B) 2 only (C) 3 only (D) 1, 2 and 3

Ans. (C)

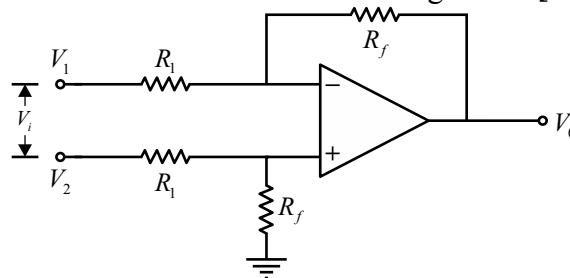
Sol.

$V_f \downarrow$	$\beta \downarrow$	$A_f \approx \frac{1}{\beta} \uparrow$
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2. OP-AMP APPLICATION (ADDER / SUBTRACTOR) :

2.1	C	2.2	1	2.3	D	2.4	A	2.5	C
2.6	B	2.7	B	2.8	A	2.9	D	2.10	C
2.11	C	2.12	A	2.13	B	2.14	B	2.15	C
2.16	A	2.17	B	2.18	C	2.19	D	2.20	C
2.21	B	2.22	B	2.23	C	2.24	B	2.25	C
2.26	C	2.27	B	2.28	1.5	2.29	15		

2.5 The differential input resistance of the circuit shown in figure is [GATE IN 1996, IISc-Bangalore]



- (A) R_1 (B) $R_1/2$ (C) $2R_1$ (D) R_f

Ans. (C)
Sol.

$$\text{Voltage at node 'b', } V_b = \frac{R_f}{R_1 + R_f} \cdot V_2$$

For ideal Op-Amp, $V_- = V_+$

$$\therefore V_a = V_b = \frac{R_f}{R_1 + R_f} \cdot V_2$$

$$\text{Current supplied by source, } I = \frac{V_a - V_1}{R_1}$$

$$\text{Differential input resistance, } R_d = \frac{V_d}{I}$$

$$I = \frac{\frac{R_f}{R_1 + R_f} \cdot V_2 - V_1}{R_1}$$

$$\text{For differential input, } V_1 = \frac{-V_d}{2}, V_2 = \frac{V_d}{2}$$

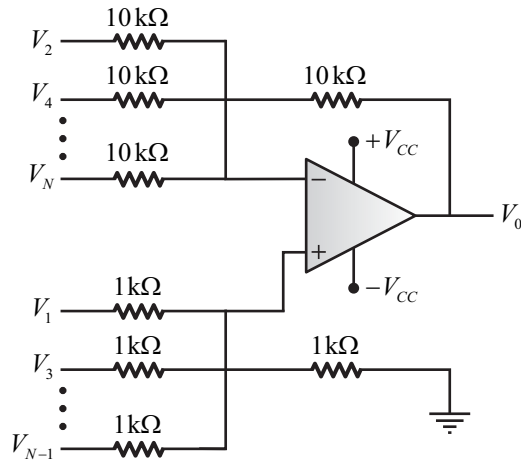
$$I = \frac{\left[\frac{1}{2} + \frac{R_f}{R_1 + R_f} \cdot \frac{1}{2} \right] V_1}{R_1}$$

$$\frac{V_d}{I} = \frac{2R_1(R_1 + R_f)}{R_1 + 2R_f} \cong 2R_1$$

2.25 Correction option (C) $-4 \cos \omega t$ V

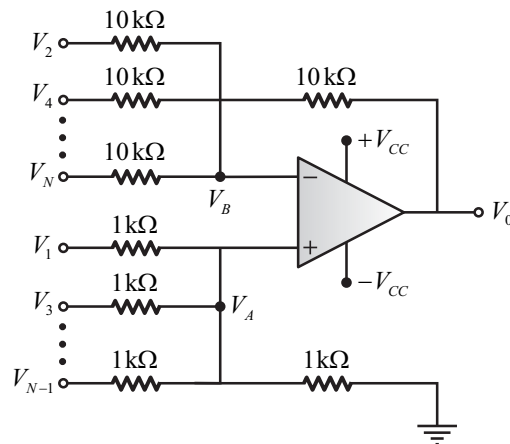
2.29 An ideal op-amp has voltage sources $V_1, V_3, V_5, \dots, V_{N-1}$ connected to the non-inverting input and $V_2, V_4, V_6, \dots, V_N$ connected to the inverting input as shown in the figure below ($+V_{CC} = 15$ volt, $-V_{CC} = -15$ volt). The voltages $V_1, V_2, V_3, V_4, V_5, V_6, \dots$ are $1, -1/2, 1/3, -1/4, 1/5, -1/6, \dots$ volt, respectively. As N approaches infinity, the output voltage (in volt) is _____.

[GATE EC 2016 (Set - 01), IISc Bangalore]



Ans. 15

Sol.



Apply nodal analysis at node A,

$$\frac{V_A - V_1}{1 \text{ k}\Omega} + \frac{V_A - V_3}{1 \text{ k}\Omega} + \dots + \frac{V_A - V_{N-1}}{1 \text{ k}\Omega} + \frac{V_A}{1 \text{ k}\Omega} = 0$$

$$V_A \left[\frac{N}{2} + 1 \right] = V_1 + V_3 + \dots + V_{N-1}$$

$$\therefore V_B = V_A \quad [\because \text{Virtual ground concept}]$$

Apply nodal analysis at node B,

$$\frac{V_A - V_2}{10 \text{ k}\Omega} + \frac{V_A - V_4}{10 \text{ k}\Omega} + \dots + \frac{V_A - V_N}{10 \text{ k}\Omega} + \frac{V_A - V_0}{10 \text{ k}\Omega} = 0 \quad [\text{We used } V_B = V_A]$$

$$V_0 = V_A \left[\frac{N}{2} + 1 \right] - (V_2 + V_4 + V_6 + \dots + V_N)$$

$$V_0 = \left[\frac{N}{2} + 1 \right] \frac{(V_1 + V_3 + \dots + V_{N-1})}{\left(\frac{N}{2} + 1 \right)} - (V_2 + V_4 + V_6 + \dots + V_N)$$

$$V_0 = V_1 - V_2 + V_3 - V_4 + \dots = 1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots$$

$$V_0 = \sum \frac{1}{N} = \infty$$

Output of op-amp goes to saturation

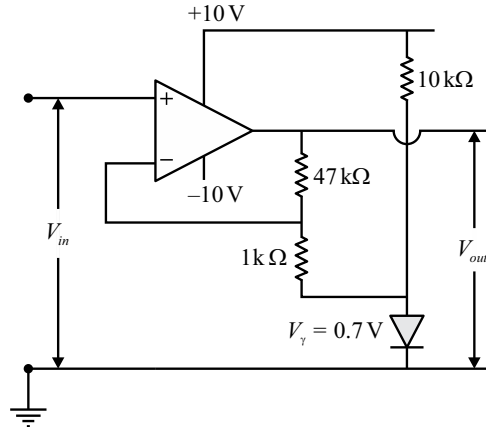
$$V_0 = V_{sat} = V_{CC} = 15 \text{ Volt}$$

Hence, the correct answer is 15.

3. OP-AMP APPLICATION (COMPARATOR / SCHMITT TRIGGER) :

3.1	D	3.2	D	3.3	D	3.4	A	3.5	A
3.6	D	3.7	A	3.8	B	3.9	B	3.10	A
3.11	B	3.12	A	3.13	B	3.14	A	3.15	D
3.16	B	3.17	C	3.18	D	3.19	A	3.20	C
3.21	C	3.22	B	3.23	C	3.24	D	3.25	D
3.26	D	3.27	D	3.28	C	3.29	D	3.30	8.10
3.31	1	3.32	A	3.33	B	3.34	0.67	3.35	D

3.9 Correction Diagram :

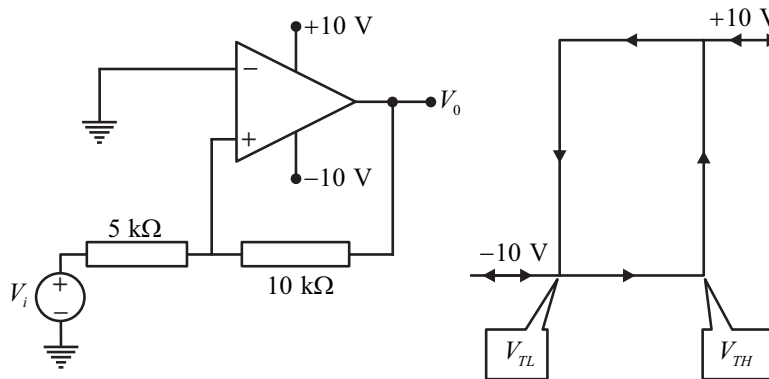


Ans. (B)

Sol. For increasing input voltage if $V_{out} = +10\text{ V}$ then triggering voltage using superposition

$$= \frac{1}{48} \times 10 + \frac{47}{48} \times 0.7 = 0.893\text{ V}$$

3.15 Shows a Schmitt trigger circuit and the corresponding hysteresis characteristics. The values of V_{TL} and V_{TH} are **[GATE IN 2004, IIT-Delhi]**



(A) $V_{TL} = -3.75\text{ V}$, $V_{TH} = +3.75\text{ V}$

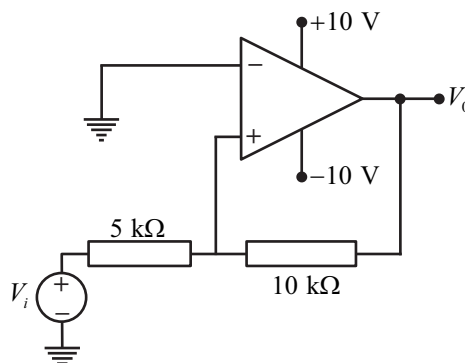
(B) $V_{TL} = -1\text{ V}$, $V_{TH} = +5\text{ V}$

(C) $V_{TL} = -5\text{ V}$, $V_{TH} = +1\text{ V}$

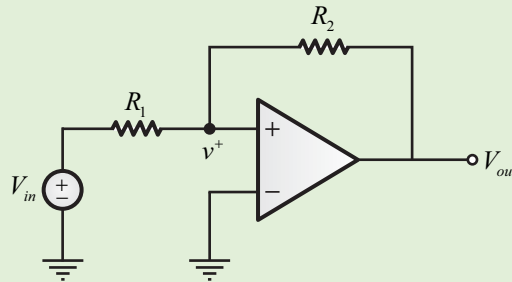
(D) $V_{TL} = -5\text{ V}$, $V_{TH} = +5\text{ V}$

Ans. (D)

Sol. Given circuit is shown below.



NON-INVERTING SCHMITT TRIGGER CIRCUIT



Op-amp with positive feedback act as a comparator and input is given to non-inverting terminal. So this is a non-inverting Schmitt trigger circuit.

Voltage v^+ is given by,

$$v^+ = \frac{V_{in} \cdot R_2}{R_1 + R_2} + \frac{V_{out} \cdot R_1}{R_1 + R_2}$$

When $V_{out} = +V_{CC}$,

$$\text{Then } v^+ = V_1 = \frac{V_{in} R_2}{R_1 + R_2} + \frac{V_{CC} R_1}{R_1 + R_2}$$

Again $V_{out} = +V_{CC}$ if $v^+ > 0$

$$\text{i.e. } \frac{V_{in} R_2}{R_1 + R_2} + \frac{V_{CC} R_1}{R_1 + R_2} > 0$$

$$V_{in} > -V_{CC} \frac{R_1}{R_2} \quad \dots\dots (i)$$

When $V_{out} = -V_{CC}$

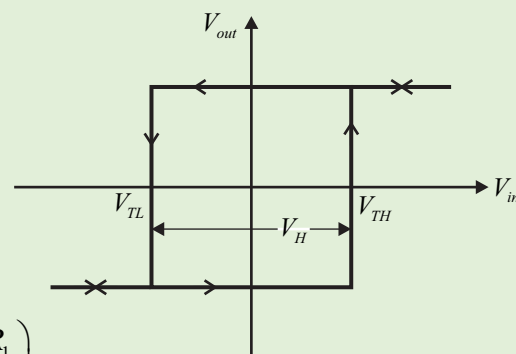
$$\text{Then } v^- = V_2 = \frac{V_{in} R_2}{R_1 + R_2} - \frac{V_{CC} R_1}{R_1 + R_2}$$

Again $V_{out} = -V_{CC}$ if $v^+ < 0$

$$\frac{V_{in} R_2}{R_1 + R_2} - \frac{V_{CC} R_1}{R_1 + R_2} < 0$$

$$V_{in} < \frac{V_{CC} R_1}{R_2} \quad \dots\dots (ii)$$

Transfer characteristics is shown below.



$$\text{Where } V_{TH} = \frac{V_{CC} R_1}{R_2} \text{ and } V_{TL} = \frac{-V_{CC} R_1}{R_2}$$

Hysteresis is given by,

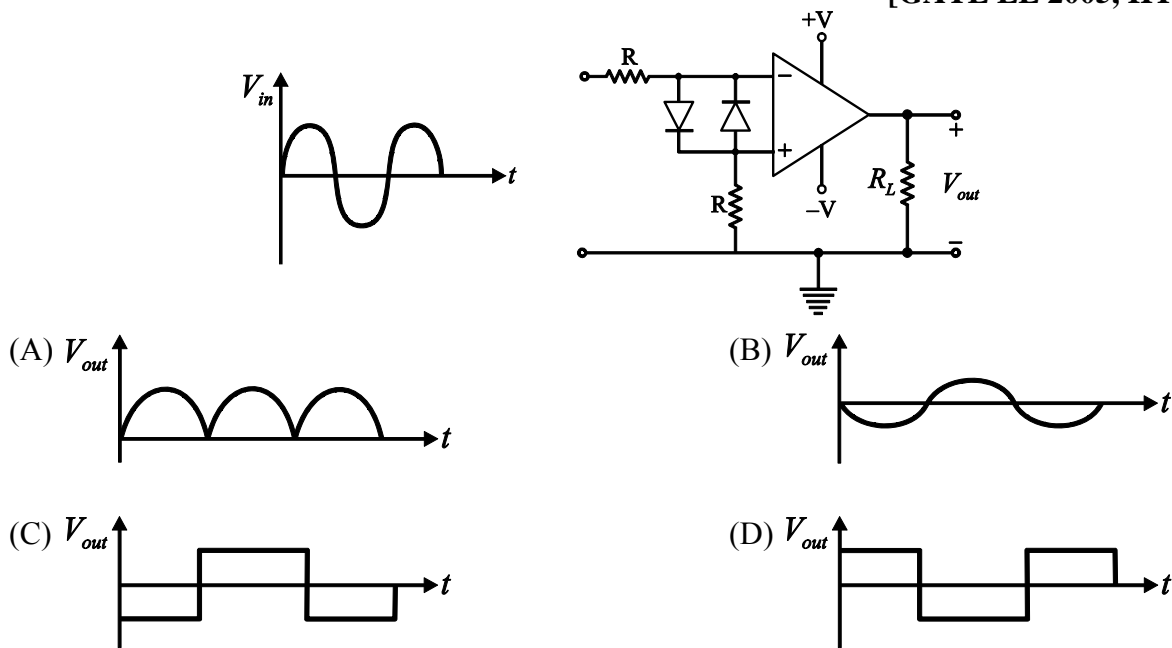
$$V_H = V_{TH} - V_{TL} = \frac{V_{CC} R_1}{R_2} - \left(\frac{-V_{CC} R_1}{R_2} \right)$$

$$V_H = 2V_{CC} \frac{R_1}{R_2}$$

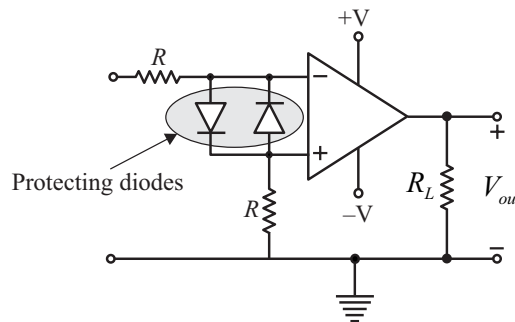
$$V_{TH} = \frac{V_{CC} R_1}{R_2} = \frac{10 \times 5}{10} = 5 \text{ V}$$

$$V_{TL} = \frac{-V_{CC} R_1}{R_2} = \frac{-10 \times 5}{10} = -5 \text{ V}$$

3.17 In the given figure, if the input is a sinusoidal signal, the output will appear as shown in [GATE EE 2005, IIT-Bombay]



Ans. (C)
Sol.



Protecting diodes are used to protect the Op-Amp from the damage due to application of high voltage.

This is an open loop system so Op-Amp behaves as a comparator.

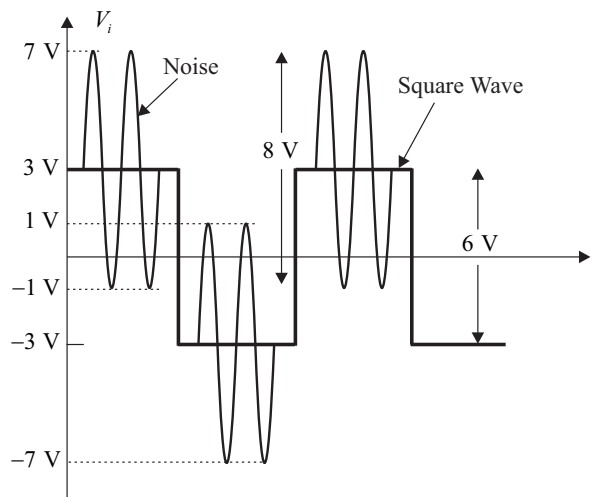
For positive half cycle, $I > NI$

$$\Rightarrow V_0 = -V_{sat}$$

For negative half cycle, $NI > I$

$$\Rightarrow V_0 = +V_{sat}$$

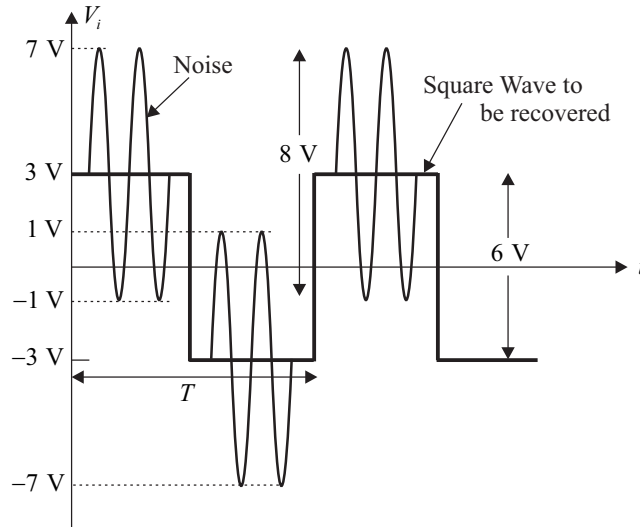
3.22 The input signal shown in the figure below is fed to a Schmitt trigger. The signal has a square wave amplifier of amplitude of 6 V p-p. It is corrupted by an additive high frequency noise of amplitude 8 V p-p. [GATE IN 2007, IIT-Kanpur]



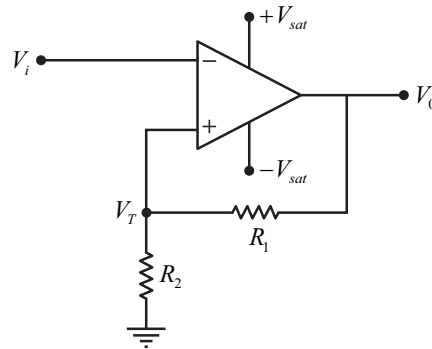
Which one of the following is an appropriate choice for the upper and lower trip points of the Schmitt trigger to recover a square wave of the same frequency from the corrupted input signal V_i ?

- (A) ± 8.0 V (B) ± 2.0 V (C) ± 0.5 V (D) 0 V

Ans. (B)
Sol.



The above corrupted signal is given as an input to Schmitt trigger circuit.



Operation of Schmitt trigger :

For $V_i > V_{UTP} \Rightarrow V_0$ switches from $+V_{sat}$ to $-V_{sat}$

For $V_i < V_{LTP} \Rightarrow V_0$ switches from $-V_{sat}$ to $+V_{sat}$

Calculation of Trip point voltage :

$$V_T = \frac{V_0 \times R_2}{R_1 + R_2} \text{ [By VDR]}$$

When $V_0 = +V_{sat}$
 $V_T = V_{UTP} =$ upper trip point

$$\therefore V_{UTP} = \frac{V_{sat} \times R_2}{R_1 + R_2} \dots\dots (i)$$

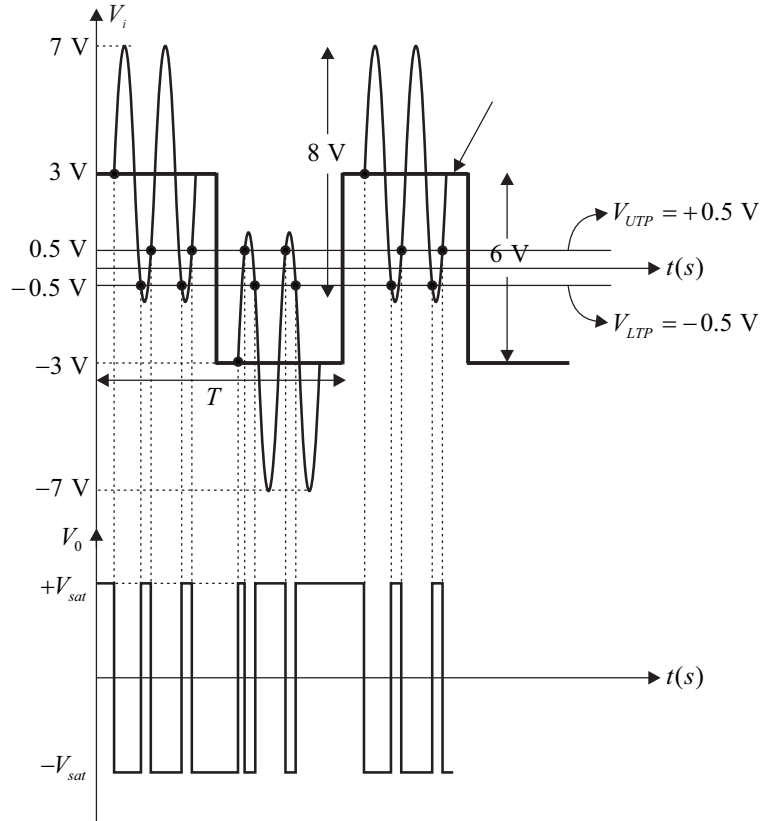
When $V_0 = -V_{sat}$
 $V_T = V_{LTP} =$ lower trip point

$$\therefore V_{LTP} = \frac{-V_{sat} \times R_2}{R_1 + R_2} \dots\dots (ii)$$

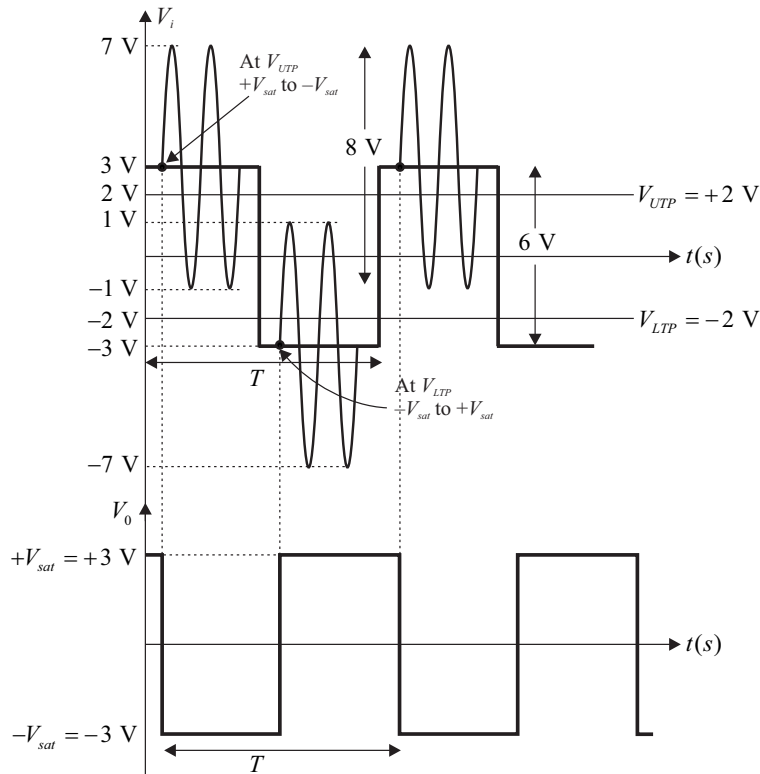
From equation (i) and (ii), we can conclude that both V_{UTP} and V_{LTP} are lesser in magnitude than $|V_{sat}|$ for proper operation.

Since the signal to be recovered is square wave of peak amplitude of +3 V. we should adjust the $\pm V_{sat}$ in such a way that it is equal to ± 3 V. (As output of Schmitt trigger is $\pm V_{sat}$.) therefore the V_{UTP} and V_{LTP} will have magnitude less than 3 V.

So, option (A) $\pm 8 \text{ V}$ is straight forwardly rejected. So now we are left with option (B), (C) and (D). Consider option (C) $\pm 0.5 \text{ V}$

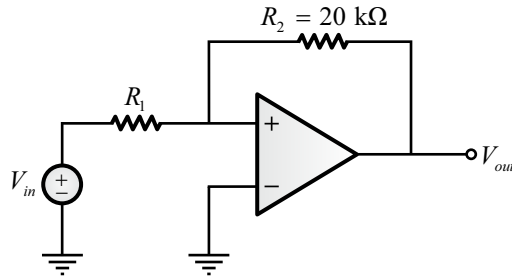


Key Point : Multiple triggering occurs if we select $|V_{UTP}|$ or $|V_{LTP}| < 1 \text{ V}$. So we can't recover square wave with same frequency because due to noise frequency will change. Consider option (B) $\pm 2 \text{ V}$



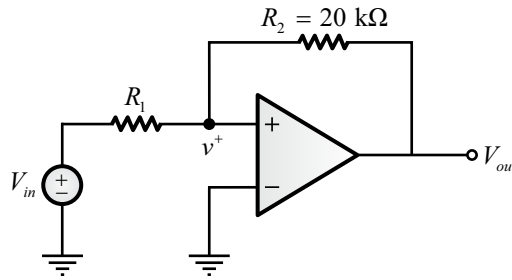
Key Point : For $|V_{UTP}|$ or $|V_{LTP}| > 1 \text{ V}$ we get square wave same as input square wave. So, $V_{UTP} = +2 \text{ V}$ and $V_{LTP} = -2 \text{ V}$ satisfies all the required conditions for recovery of square wave with same frequency. Hence, the correct option is (B).

3.31 In the bistable circuit shown, the ideal Op-Amp has saturation levels of $\pm 5\text{ V}$. The value of R_1 (in $\text{k}\Omega$) that gives a hysteresis width of 500 mV is _____. [GATE EC 2015 (Set-02), IIT-Kanpur]



Ans. 1

Sol. Given circuit is shown below.



Op-amp with positive feedback at as a comparator.

Voltage v^+ is given by,
$$v^+ = \frac{V_{in} \cdot R_2}{R_1 + R_2} + \frac{V_{out} \cdot R_1}{R_1 + R_2}$$

When $V_{out} = +V_{CC}$,

Then
$$v^+ = V_1 = \frac{V_{in} R_2}{R_1 + R_2} + \frac{V_{CC} R_1}{R_1 + R_2}$$

Again $V_{out} = +V_{CC}$ if $v^+ > 0$

i.e.
$$\frac{V_{in} R_2}{R_1 + R_2} + \frac{V_{CC} R_1}{R_1 + R_2} > 0$$

$$V_{in} > -V_{CC} \frac{R_1}{R_2} \quad \dots\dots (i)$$

When $V_{out} = -V_{CC}$

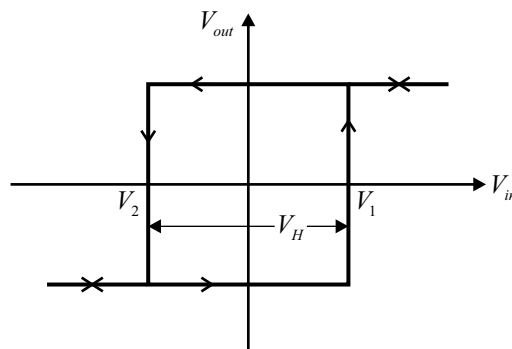
Then
$$v^- = V_2 = \frac{V_{in} R_2}{R_1 + R_2} - \frac{V_{CC} R_1}{R_1 + R_2}$$

Again $V_{out} = -V_{CC}$ if $v^+ < 0$

$$\frac{V_{in} R_2}{R_1 + R_2} - \frac{V_{CC} R_1}{R_1 + R_2} < 0$$

$$V_{in} < \frac{V_{CC} R_1}{R_2} \quad \dots\dots (ii)$$

Transfer characteristics is shown below.



Where $V_1 = \frac{V_{CC}R_1}{R_2}$ and $V_2 = \frac{-V_{CC}R_1}{R_2}$

Hysteresis is given by,

$$V_H = V_1 - V_2 = \frac{V_{CC}R_1}{R_2} - \left(\frac{-V_{CC}R_1}{R_2} \right)$$

$$V_H = 2V_{CC} \frac{R_1}{R_2}$$

Given : $V_H = 0.5 \text{ V}$

$$2 \times 5 \times \frac{R_1}{20} = 0.5$$

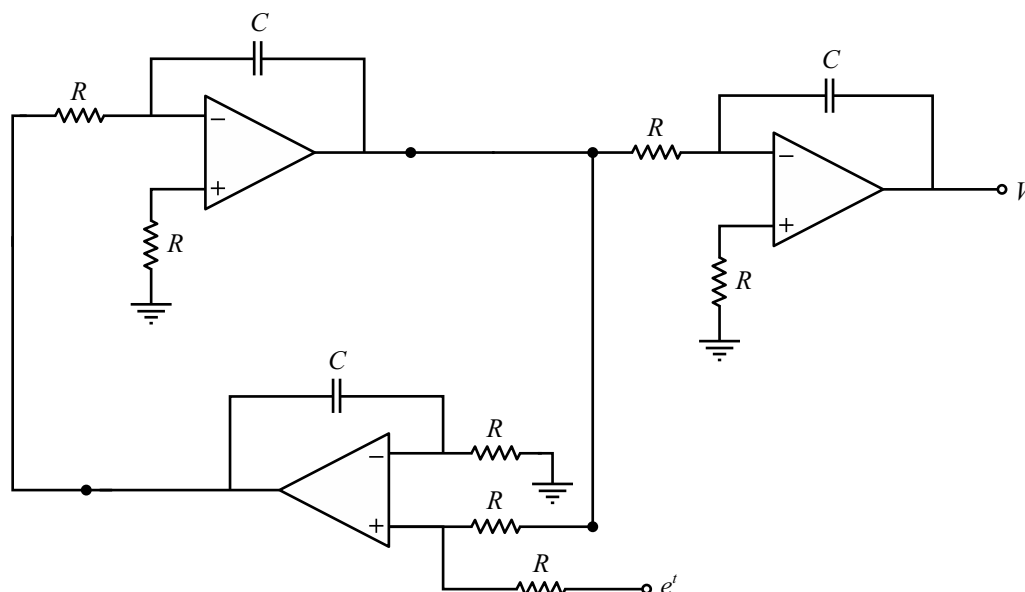
$$R_1 = 1 \text{ k}\Omega$$

4. OP-AMP APPLICATION (INTEGRATOR / DIFFERENTIATOR / ACTIVE FILTER / FREQUENCY RESPONSE) :

4.1	A	4.2	D	4.3	C	4.4	C	4.5	A
4.6	A	4.7	D	4.8	B	4.9	*	4.10	C
4.11	D	4.12	C	4.13	D	4.14	A	4.15	C
4.16	C	4.17	A	4.18	A	4.19	D	4.20	B
4.21	A	4.22	D	4.23	A	4.24	A	4.25	A
4.26	A	4.27	D	4.28	A	4.29	C	4.30	C
4.31	B	4.32	C	4.33	D	4.34	D	4.35	A
4.36	D	4.37	D	4.38	D	4.39	C	4.40	B
4.41	A	4.42	A	4.43	D	4.44	B	4.45	A
4.46	3.1-3.26	4.47	A	4.48	15-16	4.49	159.15	4.50	D
4.51	A	4.52	1.245	4.53	B	4.54	C	4.55	D
4.56	-1	4.57	A	4.58	44.37	4.59	2.95		

4.9 (A - R, B - S, C - P)

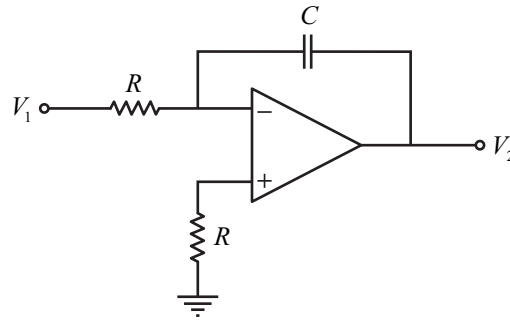
4.2 In the following circuit, the output 'V', follows an equation of the form $\frac{d^2V}{dt^2} + a \cdot \frac{dV}{dt} + bV = f(t)$. The value of a , b and $f(t)$ are respectively [GATE EE 1992, IIT-Delhi]



- (A) $a = \frac{1}{2RC}, b = \frac{1}{2R^2C^2}, f(t) = \frac{1}{2R^2C^2} \left(1 + \frac{1}{RC}\right) e^{-t}$
- (B) $a = \frac{1}{2RC}, b = \frac{1}{2R^2C^2}, f(t) = \frac{1}{R^2C^2} \left(1 + \frac{1}{RC}\right) e^{-t}$
- (C) $a = \frac{1}{RC}, b = \frac{1}{2R^2C^2}, f(t) = \frac{1}{2R^2C^2} \left(1 + \frac{1}{RC}\right) e^t$
- (D) $a = \frac{1}{2RC}, b = \frac{1}{2R^2C^2}, f(t) = \frac{1}{2R^2C^2} \left(1 + \frac{1}{RC}\right) e^t$

Ans. (D)

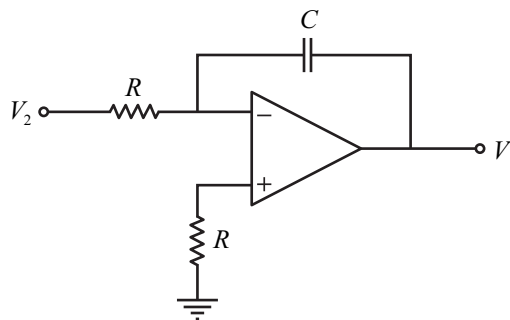
Sol. Solve the circuit in parts



Above circuit is an integrator.

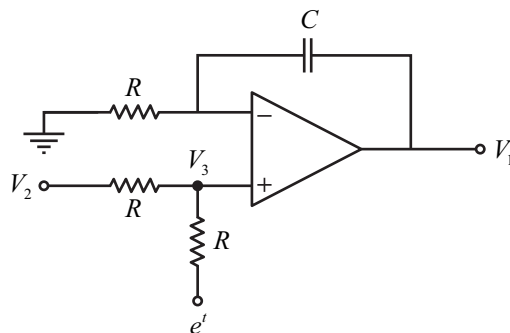
Output $V_2 = \frac{-1}{RC} \int V_1 dt$

Or $V_1 = -RC \frac{dV_2}{dt}$ (i)



Output $V = \frac{-1}{RC} \int V_2 dt$

Or $V_2 = -RC \frac{dV}{dt}$ (ii)



$$V_3 = \frac{(V_2 + e^t)}{2}$$

And $RC \frac{d}{dt} (V_1 - V_3) = V_3$

$$\text{Or} \quad RC(V_1 - V_3) = \int V_3 dt$$

$$RC(V_1 - V_3) = \frac{1}{2} \left[e^t + \int V_2 dt \right]$$

$$\text{Or} \quad RC \left[-RC \frac{d}{dt} \left(-RC \frac{dV}{dt} \right) - \left(\frac{V_2 + e^t}{2} \right) \right] = \frac{1}{2} \left[e^t + \int V_2 dt \right]$$

$$RC \left[R^2 C^2 \frac{d^2 V}{dt^2} - \frac{1}{2} e^t - \frac{1}{2} \left(-RC \frac{dV}{dt} \right) \right] = \frac{1}{2} \left[e^t - RCV \right]$$

$$\left[R^2 C^2 \frac{d^2 V}{dt^2} + \frac{1}{2} RC \frac{dV}{dt} \right] - \frac{1}{2} e^t = \frac{1}{2RC} e^t - \frac{1}{2} V$$

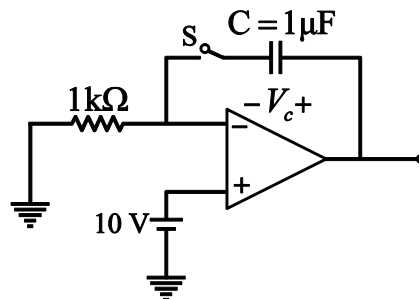
$$\text{Or} \quad R^2 C^2 \frac{d^2 V}{dt^2} + \frac{1}{2} RC \frac{dV}{dt} + \frac{1}{2} V = \frac{e^t}{2} \left(1 + \frac{1}{RC} \right)$$

Compare with

$$\frac{d^2 V}{dt^2} + a \cdot \frac{dV}{dt} + bV = f(t)$$

$$a = \frac{1}{2RC}, \quad b = \frac{1}{2R^2 C^2}, \quad f(t) = \frac{1}{2R^2 C^2} \left(1 + \frac{1}{RC} \right) e^t$$

- 4.27** For the circuit shown in the following figure, the capacitor C is initially uncharged. At $t = 0$ the switch S is closed. The voltage V_C across the capacitor at $t = 1 \text{ msec}$ is [GATE EC 2006, IIT - Kharagpur]

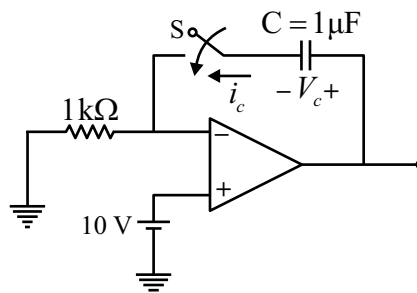


In the figures shown the OP-AMP is supplied with $\pm 15 \text{ V}$.

- (A) 0 V (B) 6.3 V (C) 9.45 V (D) 10 V

Ans. (D)

Sol.



Above figure represents the linear charging of capacitor. Here transient equation is not valid.

After closing the switch apply KCL at non-inverting terminals.

Due to virtual ground

$$V_+ = V_- = 10\text{ V}$$

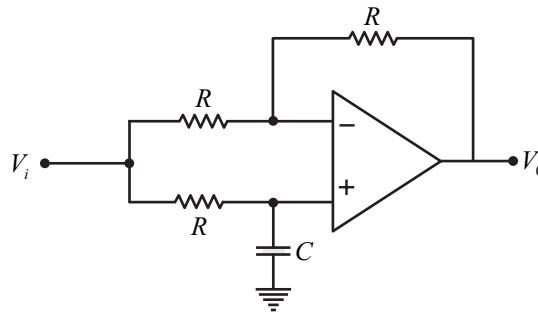
$$i_c = \frac{10}{1\text{ k}}$$

$$c \frac{dV_c}{dt} = \frac{10}{1\text{ k}}$$

$$\frac{10^{-6} \times V_c}{1 \times 10^{-3}} = \frac{10}{10^3}$$

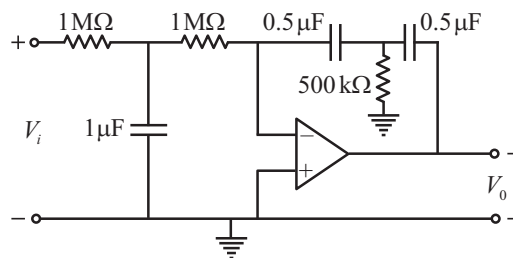
$$V_c = 10\text{ Volt}$$

4.28 and 4.29 Common data Correction diagram



4.39 The ideal Op-Amp based circuit shown below acts as a

[GATE IN 2011, IIT-Madras]

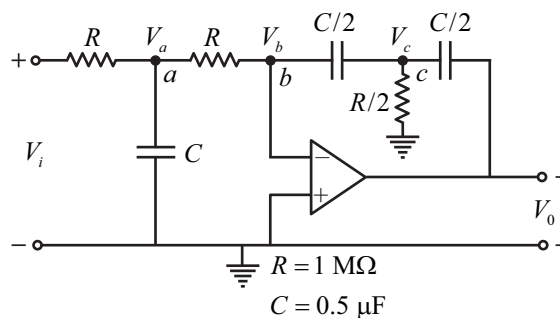


- (A) low-pass filter
- (C) band-pass filter

- (B) high-pass filter
- (D) band-reject filter

Ans. (C)
Sol.

Method 1



The type of filter can be determined from the transfer function of circuit in s-domain. So transfer function of circuit will be obtained first. From which conclusion will be draw about type of filter.

KCL at node (a),

$$\frac{V_a - V_i}{R} + \frac{V_a - V_b}{R} + \frac{V_a - 0}{1/sC}$$

As node 'b' is at virtual ground, so $V_b = 0$

$$V_a \left[\frac{2}{R} + sC \right] = \frac{V_i}{R}$$

$$V_a = \frac{V_i}{2 + sCR} \dots\dots (i)$$

KCL at node (b),

$$\frac{0 - V_a}{R} + \frac{0 - V_c}{2/sC} = 0$$

$$V_a = -\frac{sCR}{2} V_c \quad \dots\dots (ii)$$

From equation (i) and (ii), we have

$$-\frac{sCR}{2} V_c = \frac{1}{2 + sCR} V_i$$

$$V_c = -\frac{2}{sCR(2 + sCR)} \times V_i \quad \dots\dots (iii)$$

KCL at node (c),

$$\frac{V_c - 0}{2/sC} + \frac{V_c}{R/2} + \frac{V_c - V_0}{2/sC} = 0$$

$$V_c \left[sC + \frac{2}{R} \right] = \frac{sCV_0}{2}$$

$$V_c = \frac{sCR}{2(2 + sCR)} V_0 \quad \dots\dots (iv)$$

From equation (iii) and (iv), we have

$$\frac{sCR}{2(2 + sCR)} V_0 = -\frac{2}{sCR(2 + sCR)} \times V_i$$

$$\frac{V_0}{V_i} = -\frac{4}{(sCR)^2}$$

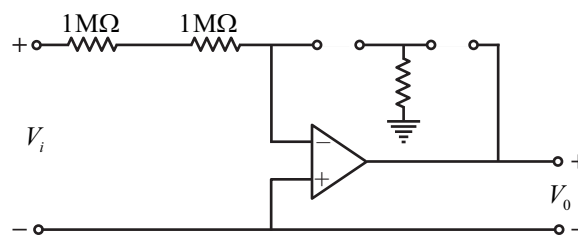
In frequency domain, $s = j\omega$

$$\therefore \frac{V_0}{V_i} = \frac{4}{\omega^2 CR}$$

Gain of circuit reduces as ω increases so given filter like low pass filter.

Method 2

At low frequency $f = 0, X_C = \infty, C \rightarrow O.C.$



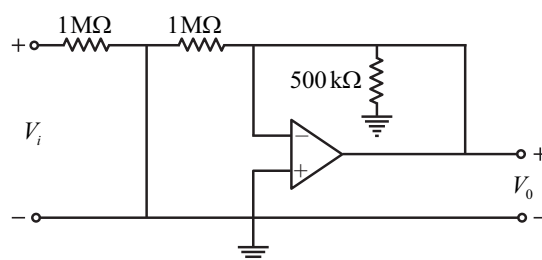
This is an open loop system. So, Op-Amp behaves as a comparator.

$$\therefore \text{if } V_i > 0 \Rightarrow V_0 = -V_{sat}$$

$$\text{If } V_i < 0 \Rightarrow V_0 = +V_{sat}$$

In this case $V_0 = |V_{sat}| = \text{finite gain}$

At high frequency $f = \infty, X_C = 0, C \rightarrow S.C.$

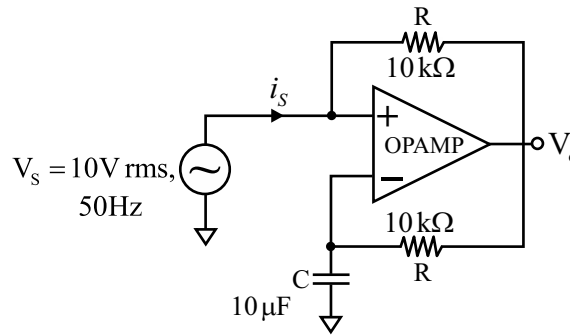


Here $V_0 = 0$ (Due to virtual ground)

So, this circuit act as a low pass filter.

4.42 The following circuit has $R = 10\text{ k}\Omega$, $C = 10\text{ }\mu\text{F}$. The input voltage is a sinusoidal at 50Hz with an rms value of 10 V. Under ideal conditions, the current i_s from the source is

[GATE EE 2009, IIT-Roorkee]



(A) 10π mA leading by 90°

(B) 20π mA leading by 90°

(C) 10 mA leading by 90°

(D) 10π mA lagging by 90°

Ans. (A)

Sol.

$$V_s = \left(\frac{X_c}{R + X_c} \right) V_0$$

Where

$$X_c = \frac{-j}{\omega C}$$

and

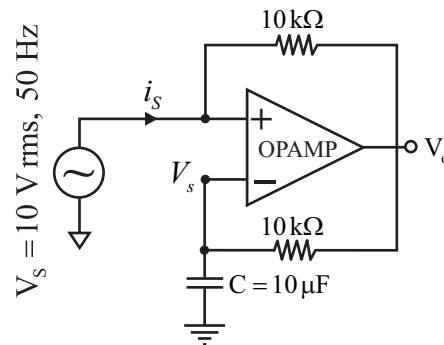
$$i_s = \frac{V_s - V_0}{R} = \frac{V_s - \left(\frac{R + X_c}{X_c} \right) V_s}{R}$$

$$i_s = \frac{-RV_s}{RX_c} = -V_s j\omega C$$

$$i_s = -j(2\pi \times 50 \times 10 \times 10^{-6})$$

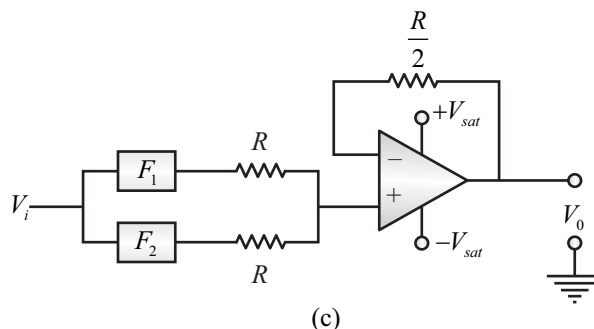
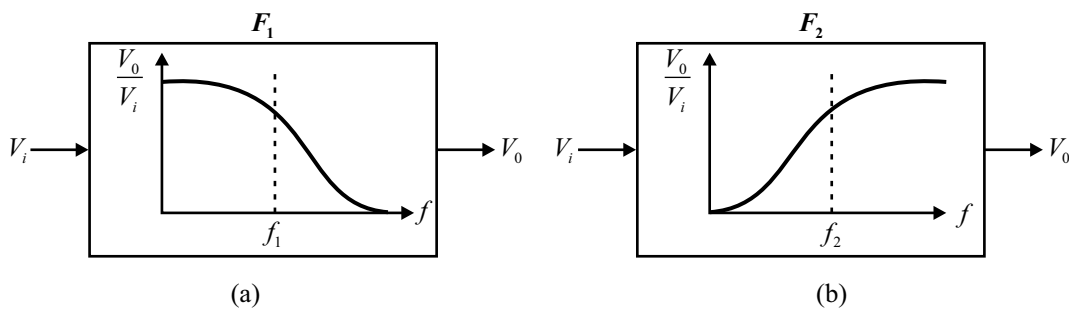
$$i_s = -j10\pi \text{ mA}$$

So, 10π mA lagging by 90° .



4.53 The filters F_1 and F_2 having characteristics as shown in figure (a) and (b) are connected as shown in figure (c).

[GATE EE 2015 (Set-02), IIT-Kanpur]



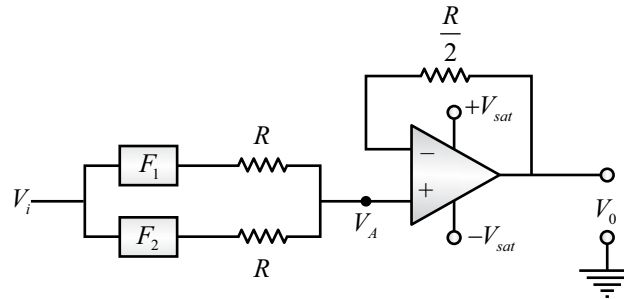
The cut-off frequencies of F_1 and F_2 are f_1 and f_2 respectively. If $f_1 < f_2$, the resultant circuit exhibits the characteristic of a

- (A) Band-pass filter (B) Band-stop filter (C) All pass filter (D) High- Q filter

Ans. (B)

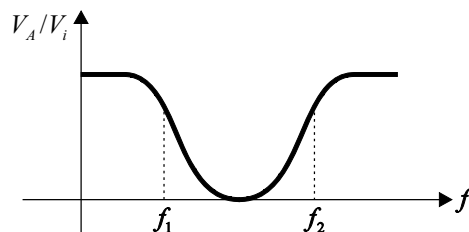
Sol. The given circuit represents F_1 as LPF & F_2 as HPF in parallel followed by a buffer.

LPF will pass all the frequencies less than f_1 and HPF pass all the frequencies above f_2 .



Since $f_1 < f_2$; frequencies lying between f_1 and f_2 will be stopped.

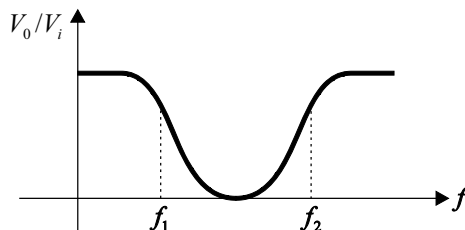
Since $f_1 < f_2$, so V_A/V_i will be



From figure $V_0 = V_a$ (voltage follower circuit)

So
$$\frac{V_0}{V_i} = \frac{V_a}{V_i}$$

V_0/V_i will be



Hence the circuit behaves like a band stop filter.

